

A large, high-contrast black and white photograph of an explosion serves as the background. A massive, billowing cloud of smoke and fire dominates the center-left, with bright light emanating from the core. To the right, a smaller, more structured explosion is visible, showing sparks and debris. The overall scene is dramatic and intense.

MUNITION VULNERABILITY SIMULATION TOOLBOX

Gert Scholtes

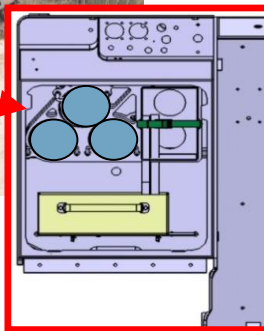
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OVERVIEW

- Background and approach
- Shock initiation modelling
- Validation and comparison
- Energy fluence E_c
- Influence of additional layer
- Future: Vulnerability toolbox / user interface
- Conclusions

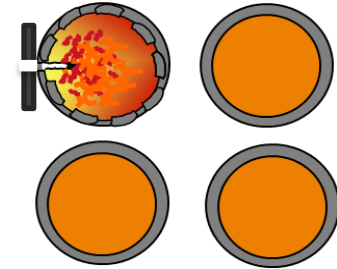
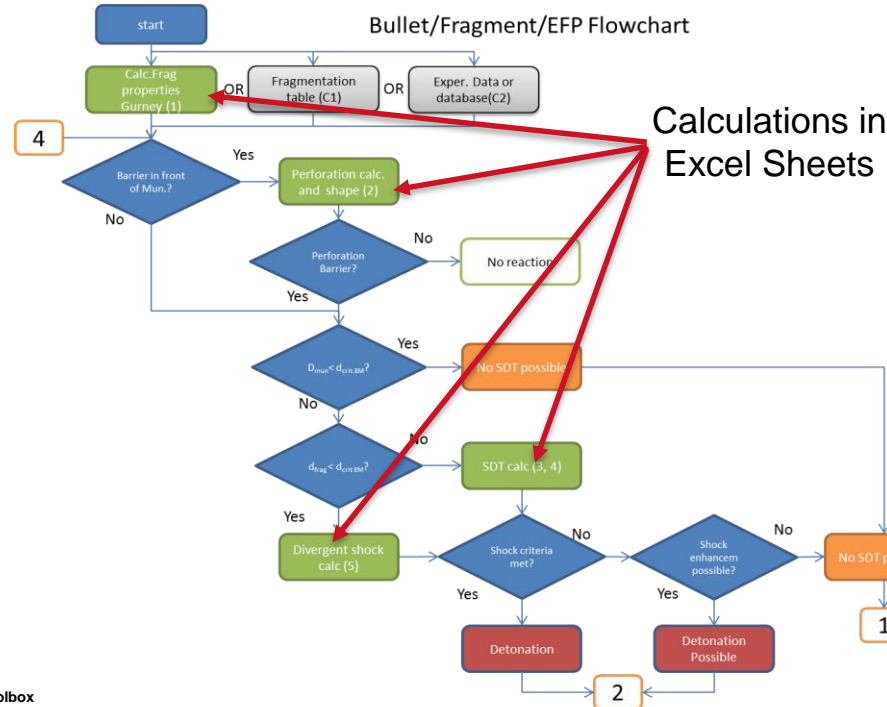
BACKGROUND AND APPROACH

LIFE-CYCLE MUNITIONS - THREATS



- Fragments
- SCJ
- Bullets
- Cook-off
- Sympathetic reaction

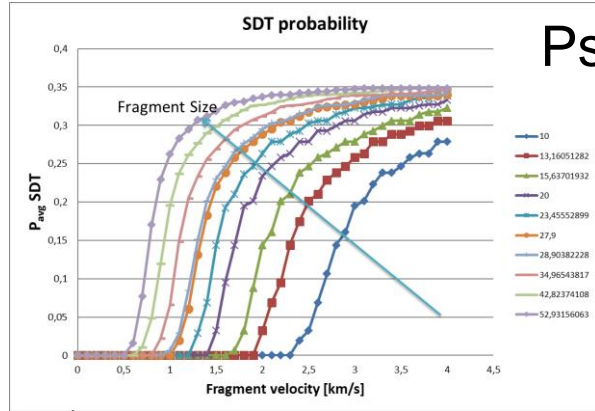
TNO APPROACH MUNITION VULNERABILITY TOOLBOX THREAT – DONOR - ACCEPTOR



- Spreadsheets/comments:
- (1) Fragment velocity calculation with Gurney
 - (2) Perforation calculation using Thor equations
 - (3) SDT calculation Ec theory Haskins and Cook
 - (4) SDT calculation Green or Lundstrom
 - (5) Divergent shock calculation Green/Lundstrom
 - (6) EM heating due to penetration
 - (7) EM cook-off reaction calculation after penetration of bullet
 - (8) Pressurisation calculation after ignition and burning of EM
 - (9) Sympathetic reaction calculation confined stack and on-on-one
 - (10) TNT equivalent blast/shock calculation
 - (C1) Fragmentation table of munitions (table #.#)
 - (C2) Fragmentation data from experiments or databases
 - (C3) Bullet and fragment test result database (e.g. BIRD or FRAID)
 - (C4) SG table ref [H] tabel #.#
 - (C5) Cook-off database test results
- Excel spreadsheet calculation
 - Excel spreadsheet not implemented
 - Excel spreadsheet (needs data)
 - Data from database or Experiments
 - Detonation reaction (possible)
 - No Prompt shock detonation (SDT)
 - Decision
 - Reference Number

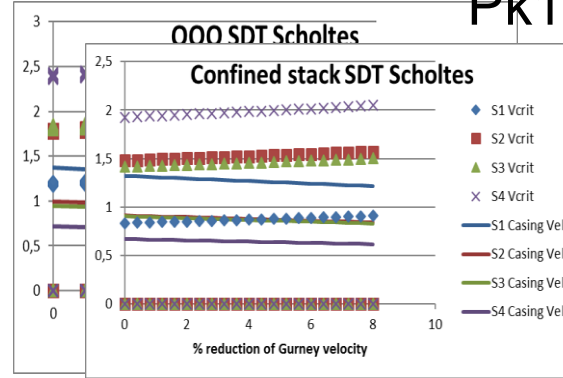
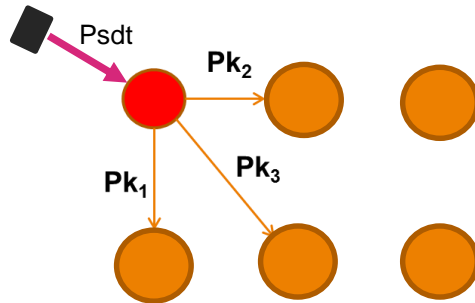


EXAMPLE: PROBABILITY OF A SR



P_{sdt}

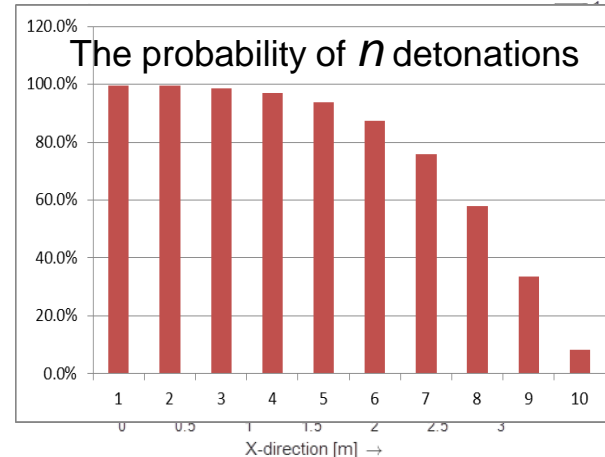
Fragment



P_{k1}, P_{k2}

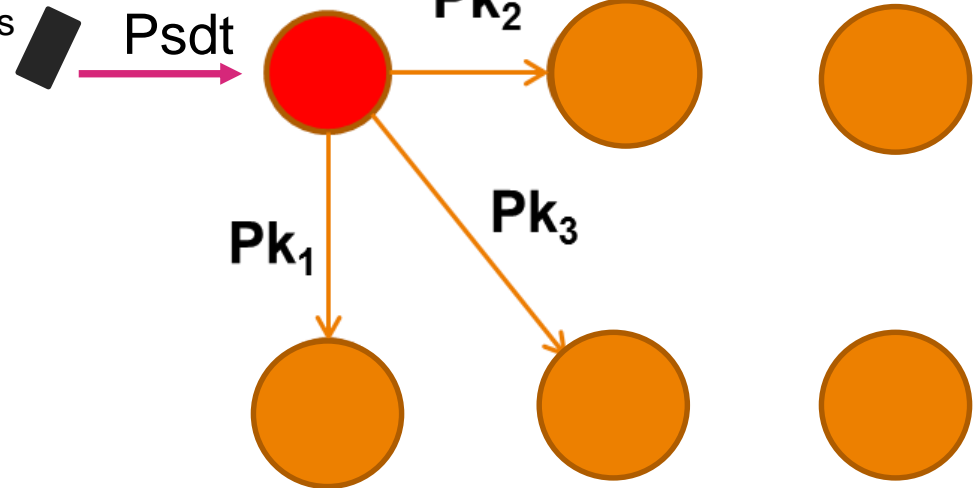
P_{k3}

Probability of detonation of Shells in Rack



SCENARIO - PROBABILITY

- › E.g. missile hit: fragments travelling towards munition storage
- › Probability: need for thousands of calculations
- › Simple equation i.s.o. Hydro-code calculations



Need for good estimate of
 $V_{crit-frag}$ with Shock model

SHOCK INITIATION MODELLING

JACOBS-ROSLUND SHOCK MODEL: V_{CRITICAL} FOR COVERED EXPLOSIVES

› Important parameters Required:

- › Fragment diameter d
- › Thickness of casing t
- › Sensitivity of Explosive A

› **Positive**

- › Data for many explosives

› **Negative**

- › Only steel fragment and casing
- › No other layer e.g. Asphalt or PU liners

$$\begin{cases} V_1 = \frac{A}{d^\beta} (1 + B)(1 + C \frac{t}{d}) & \text{for } d > d_c \\ V_2 = \frac{E}{d^\alpha} & \text{for } d < d_c \end{cases} \quad (3)$$

where $V_{\text{threshold}}$ = critical impact velocity for target detonation (mm/ μ s) = max (V_1 , V_2)

d = fragment critical dimension e.g. diameter (mm)

β = exponent equal to $\frac{1}{2}$ in the original equation

α = exponent added in a further improvement to the original formula

d_c = explosive critical diameter

t = target cover thickness (mm)

A = explosive sensitivity coefficient (mm^{3/2}/ μ s)

B = fragment shape coefficient (dimensionless)

$B = 0$ for flat ended cylinder

$B = 1$ for sphere

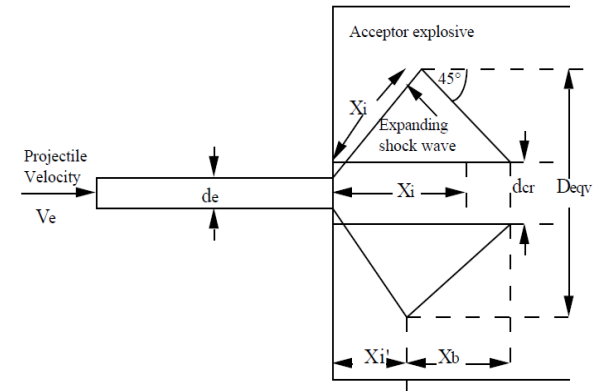
C = cover plate protection coefficient (dimensionless). C is different for blunt cylinders and spheres: $C_{\text{sphere}} = 1/3 C_{\text{cylinder}}$.

E = explosive sensitivity second coefficient

GREEN SHOCK MODEL

- › Uses pop-plot data of explosive; characteristic data P_1 and S (run distance to detonation) and critical diameter of explosive
- › Method: what pressure P_e will lead to a detonation due to shock wave having a diameter $\geq D_{crit}$, detonation at depth X , in the explosive
- › Also model when Diameter impactor $< D_{crit}$, explosive
- › **Positive**
 - › Relative large database for different explosives
- › **Negative**
 - › Results do not always connect (range $D_{frag} < D_{crit,expl}$ with $D_{frag} > D_{crit,expl}$)
 - › Not for spheres or oblique impact

$$X = 10 \left(\frac{P_1}{P_e} \right)^S$$

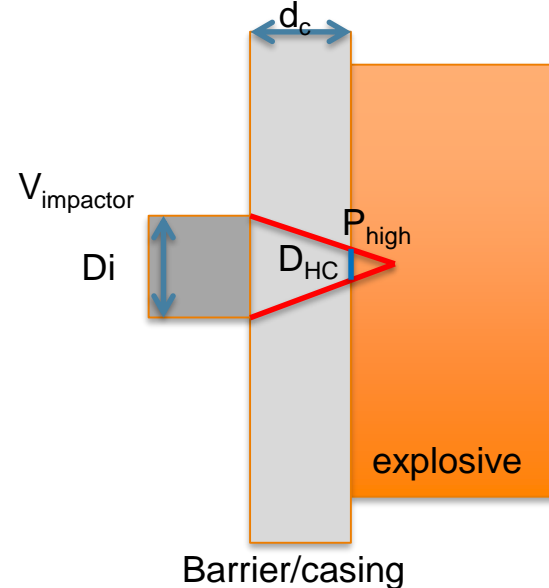


OLD JAMES, HASKINS AND COOK BASED ON E_c

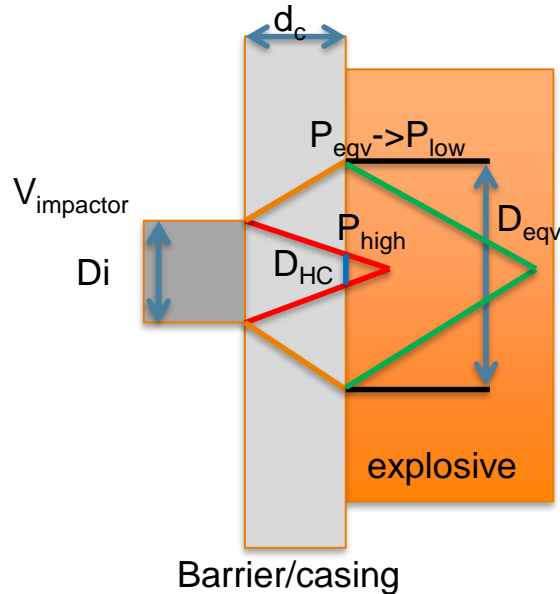
- › Uses shock Hugoniot and E_c for sensitivity of explosive, diameter and velocity fragment
- › (T = shock duration, u_p particle velocity P the pressure
- › Pressure and particle velocity u_p depend on fragment velocity and shock hugoniot of materials
- › Method: solve V_{crit} for $E_{frag}=E_c$
- › **Positive**
 - › Model can be used for all kind of cover materials
 - › Also for spheres or oblique impact
 - › One value of E_c
- › **Negative**
 - › Not always correct value (high velocities)
 - › Does not work if $D_{frag} < 2 \cdot D_{casing}$ (thickness)

$$E = \int P \cdot u_{p,x} \cdot dt \quad \text{or} \quad E_c = P u_p T$$

$$T = \frac{R_c}{3c} \quad E_c = \frac{P u_p R_c}{3c}$$



NEW SHOCK MODEL: COMBINATION OF JH&C AND P_{EQV} IDEA OF GREEN $\rightarrow E_{FLUX}$



Energy Fluence:
$$E = \int P \cdot u_{p,x} \cdot dt$$

With: P = pressure in the explosive, $u_{p,x}$ Part. Velocity of explosive and t the time of the shock duration

For explosive $E_{impactor} \geq E_{crit,exp} \rightarrow$ Detonation

- › Solving impedance matching equations for projectile \rightarrow barrier \rightarrow explosive

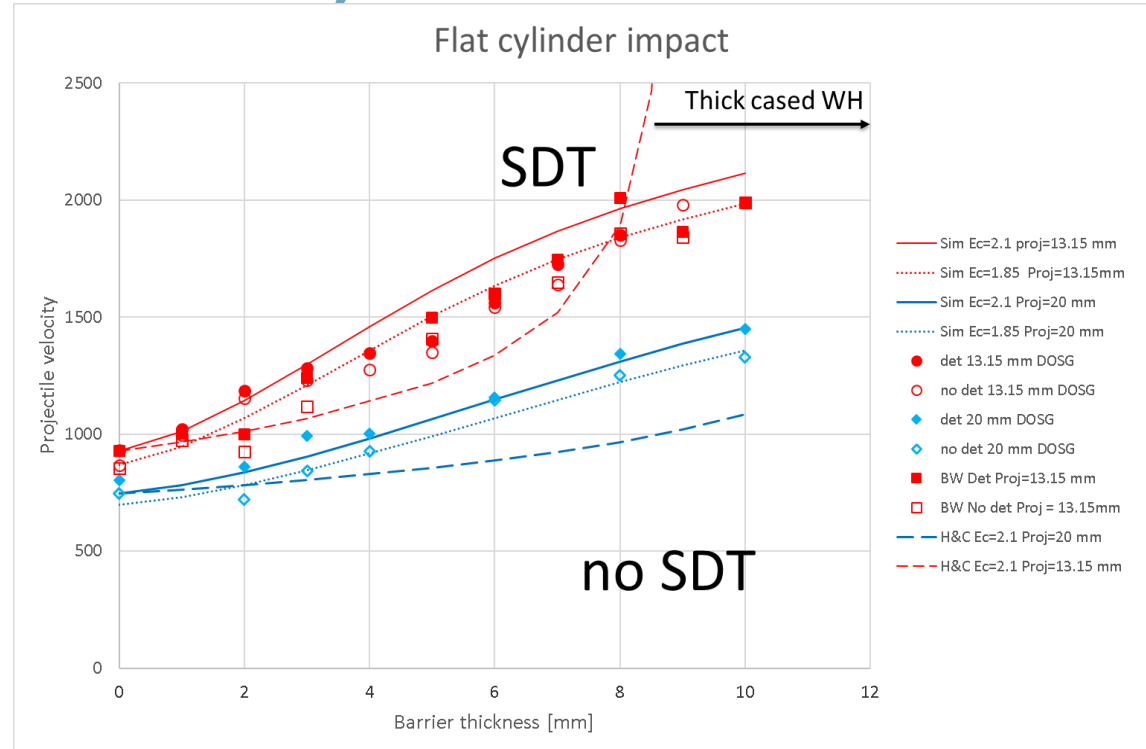
$$E_{total} = \frac{\{ E_{expanding} \pi [(D_{eqv}/2)^2 - R_c^2] + E_{H\&C} \pi R_c^2 \}}{\{ \pi (D_{eqv}/2)^2 \}}$$

$E_c = E_{total}$ › Solving equation $\rightarrow V_{critical, projectile}$

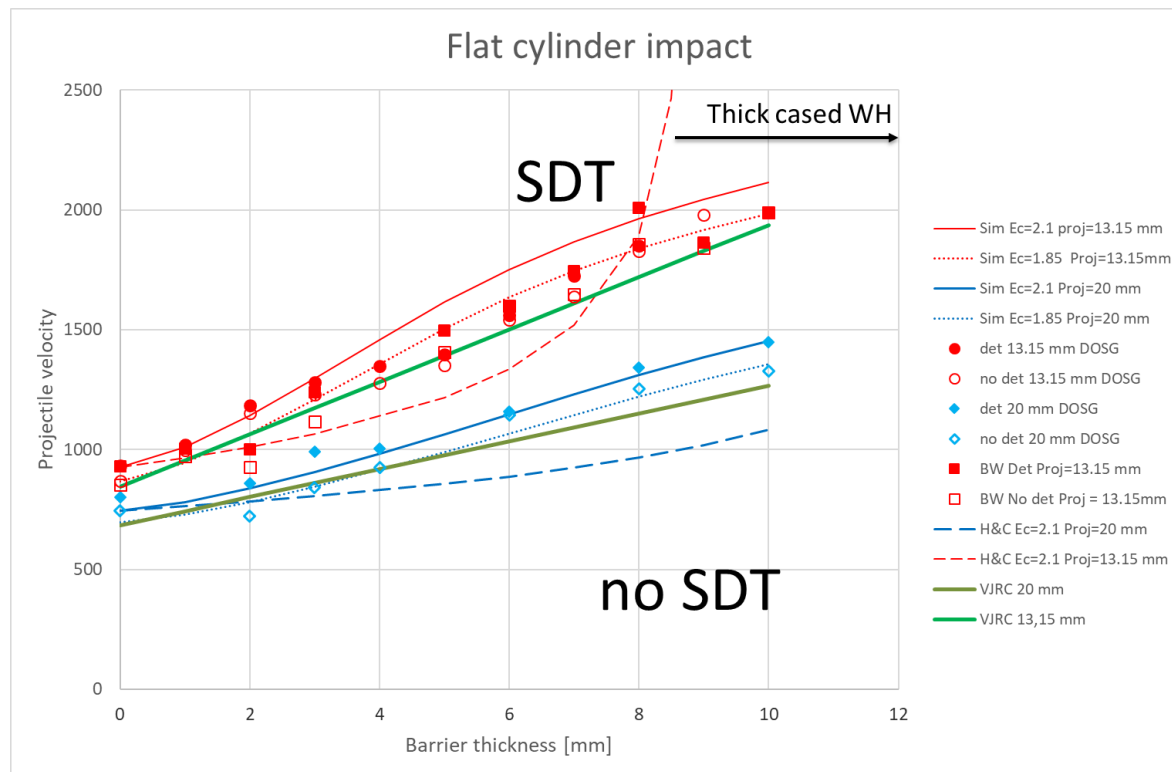
VALIDATION AND COMPARISON

VALIDATION WITH DATA FROM LITERATURE (EXAMPLE: COMPOSITION B)

- › Value E_c influenced by type of study:
 - › Vulnerability or
 - › Lethality

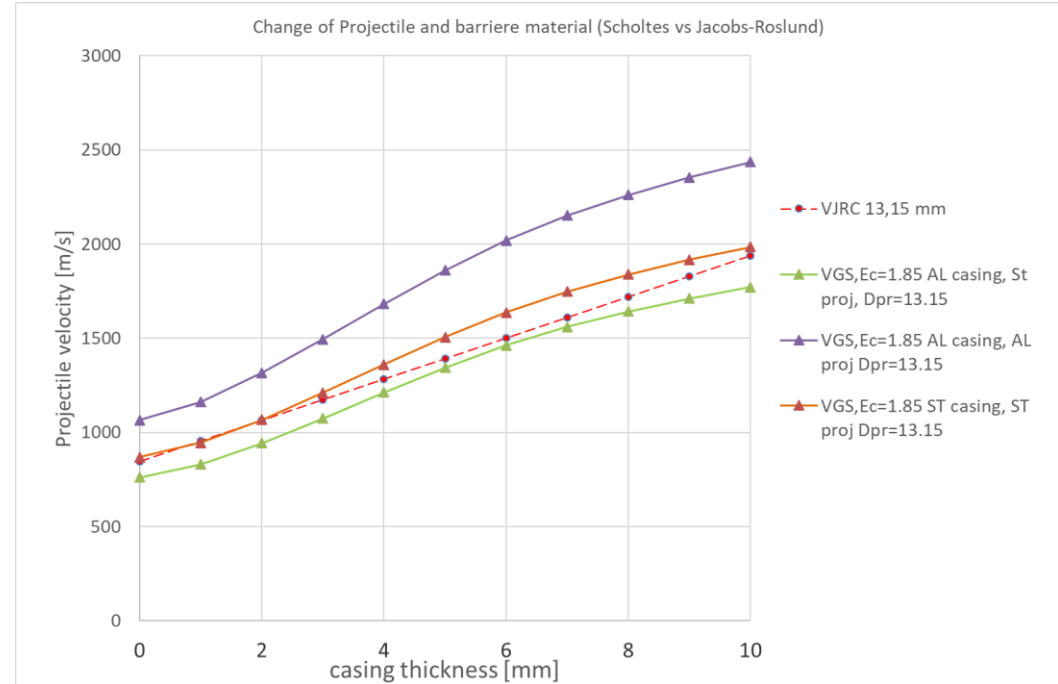


EXPERIMENTAL VS. JR VS. H&C VS. SCHOLTES



WHY JACOBS-ROSLUND NOT ALWAYS GOOD OPTION?

- › Comp B: Steel proj, steel casing
- › Comp B: steel proj, Aluminium casing
- › And what if:
- › Comp B: Alum proj. and Alum casing?



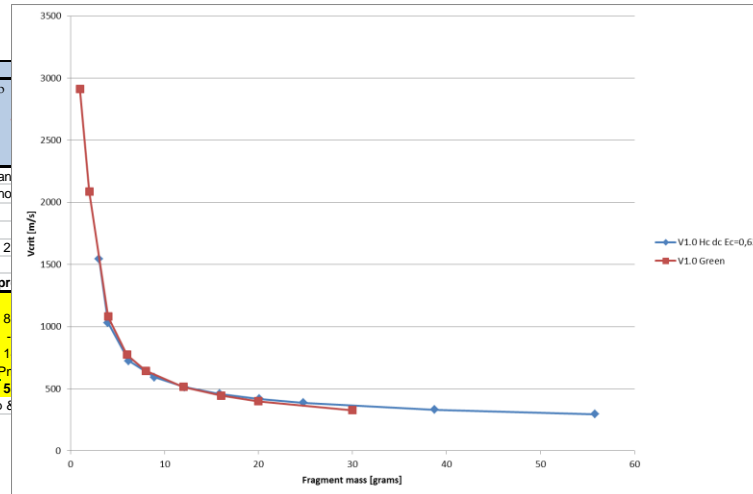
ENERGY FLUENCE E_c

ESTIMATION OF VALUE OF E_c : COMPARISON WITH OTHER MODELS

- Haskins and Cook use Critical Energy criteria E_c (shock mechanics)
- Green/Lundstrom uses critical diameter D_c of explosives and Run-distance to detonation criteria:
- With P_1 and S the characteristic parameters of an explosive

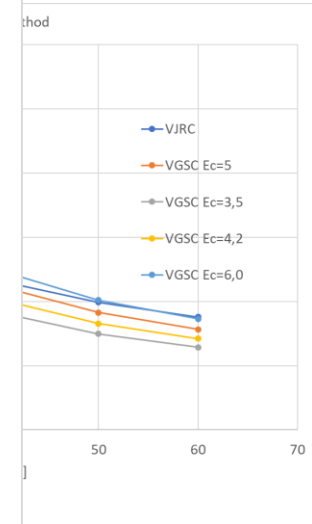
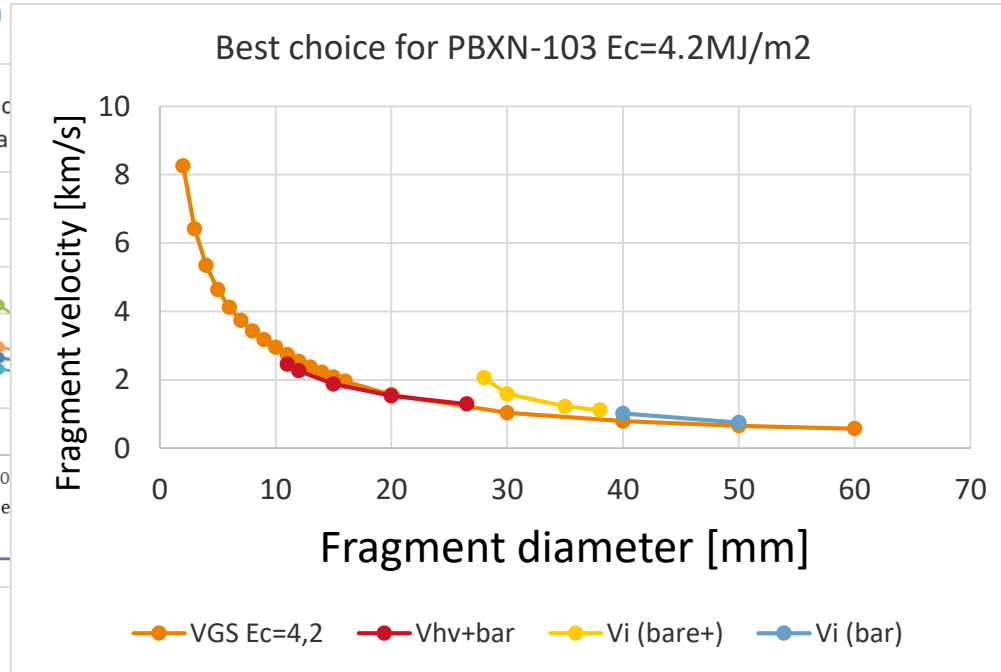
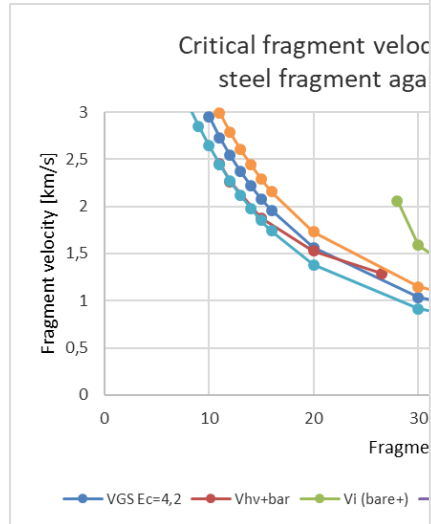
$$X = 10 \left(\frac{P_1}{P_e} \right)^S$$

Hugoniot calculations			
Us=Co+sUp	Co	S	p
staal	4,58	1,49	
staal	4,58	1,49	
Comp B	3,03	1,73	
PBX9404	2,46	2,5300001	
Imp vel, km/s	2,6086	km/s	an
Imp vel, km/s	2,2591	km/s	no
check angel		2,259	2
pr			
Quadratic solutions for up			
a=	-1E-07	a=	8
b=	-125,4	b=	-
c=	141,63	c=	1
Up match	Pr		
1,1295596	5		
1st match up	6		



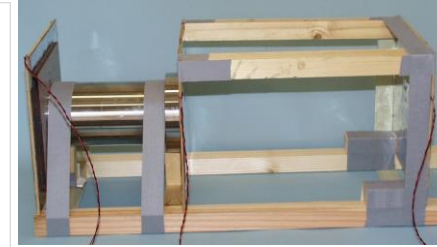
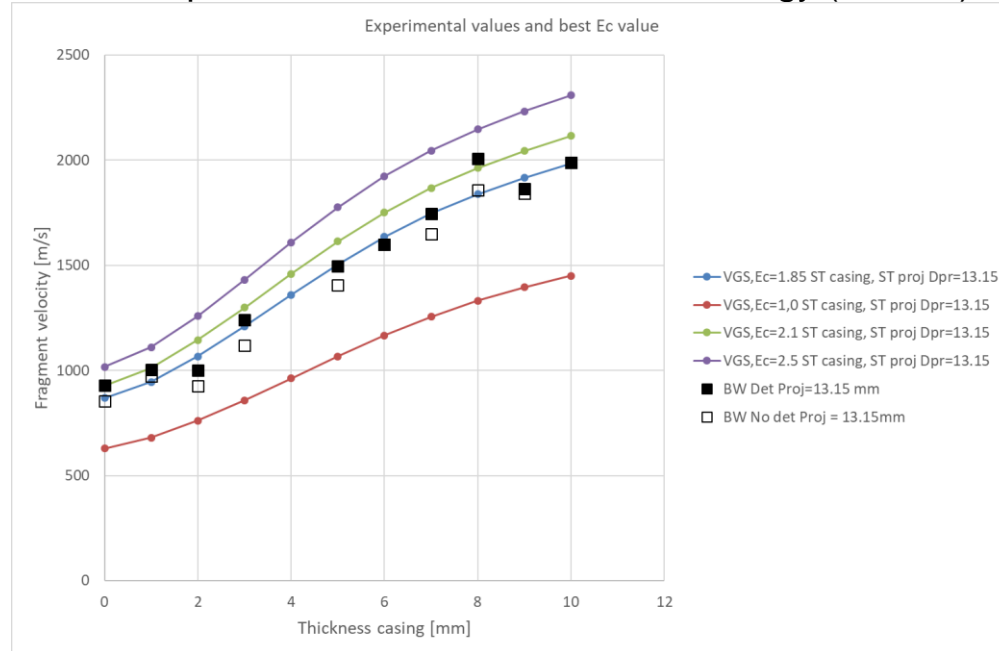
4,32	Uit green shock methode gebruik van methode price [1		
det sym.			
(haskins8	2,55466838	micro-sec	
71016897		flat nose	1
		165° cone	1
vormfactor	2,7	150° cone	1,5
		135° cone	1,9
		120° cone	2,7
		bol	3
dcritisch=25,2 mm			
Hc di=1	dc=4	Hc di=1,5	dc=4
0		vi (green)	
0			

EXAMPLE PBXN-103; GREEN AND JR VERSUS NEW MODEL

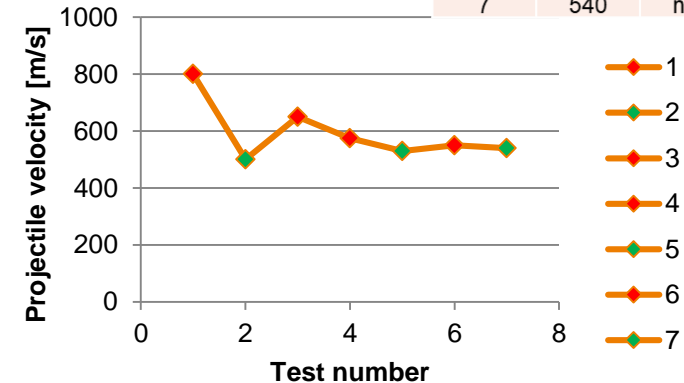


EXPERIMENTS: V_{CRIT} AS FUNCTION OF PROJECTILE DIAMETER OR BARRIER THICKNESS

› From experiments estimation of critical Energy (fluence) E_c



Test #	Proj V	Reaction
1	800	Detonation
2	500	no-D
3	650	D
4	575	D
5	530	no-D
6	550	D
7	540	no-D



NEW METHOD FOR E_c : REACTION ZONE LENGTH δ

$$E_c = \frac{\rho_o D_j \delta \left[\frac{D_j - a_x}{2b_x} + \frac{D_j}{2(r+1)} \right]^2}{D_j - \left(\frac{D_j - a_x}{2b_x} + \frac{D_j}{2(r+1)} \right)} \quad 1)$$

- › Shock Hugoniot of material: $U_s = a_x + b_x U_p$
- › D_j = detonation velocity
- › r = Specific heat ratio
- › ρ_o = density of explosive
- › δ = length of reaction zone \rightarrow to be determined

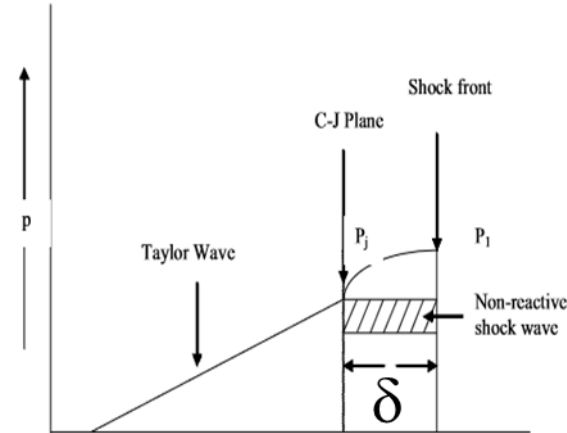


Table 3. Comparison of calculated and reported values of critical shock energies of different explosives

S.No.	Explosive	Density g/cc	Critical shock energy E_c , J/cm ²		Reference No.
			Calculated	Reported	
1.	RDX/TNT (60/40)	1.72	201.80	190.0	4
2.	TNT	1.54	83.50	77.0	4
3.	HMX	1.77	153.89	150.0	2
4.	RDX	1.60	174.30	175.0	2

¹⁾ H.S. Yadav, S.N. Asthana, and A. Subhananda Rao,
Critical Shock Energy and Shock and Detonation Parameters of an Explosive
Defence Science Journal, Vol. 59, No. 4, July 2009, pp. 436-440

REACTION ZONE MEASUREMENT USING SHOCK INDUCED POLARIZATION ¹⁾

- › Works good up to pressures of 25 GPa in Plexiglas, but maybe other materials can be used

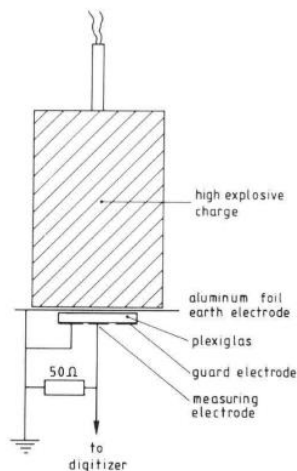


Fig. 1. Setup of shock-induced polarization experiments behind high explosives.

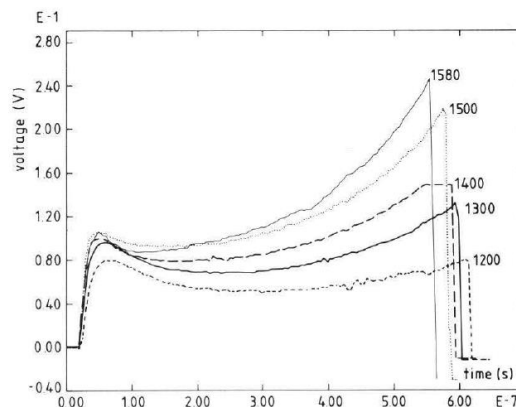


Fig. 5. SIP signals from 3 mm Plexiglas behind TNT charges pressed to five different densities (indicated in kg/m^3).

TABLE I

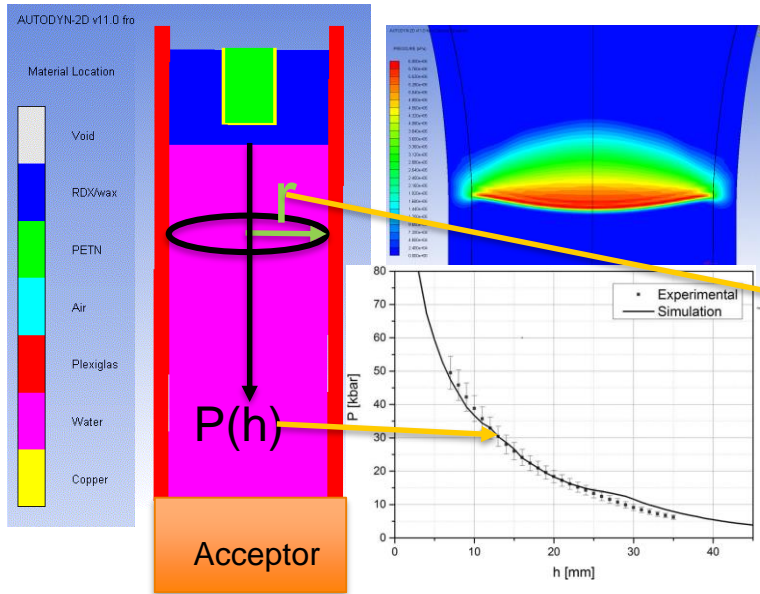
Reaction Zone Parameters and Detonation Velocity for Pressed TNT Charges of Various Densities

Density (kg/m^3)	Reaction Time (ns)	Detonation Velocity (m/s)	Reaction Zone Length (mm)
1200	251	5300	0.93
1300	205	5700	0.82
1400	134	6240	0.59
1500	110	6490	0.50
1580	81	6830	0.39

¹⁾R. R. IJsselstein, *Reaction zone measurements in high explosive detonation waves by means of shock-induced polarization*, *Combustion and Flame*, 66 (1986) 27-35

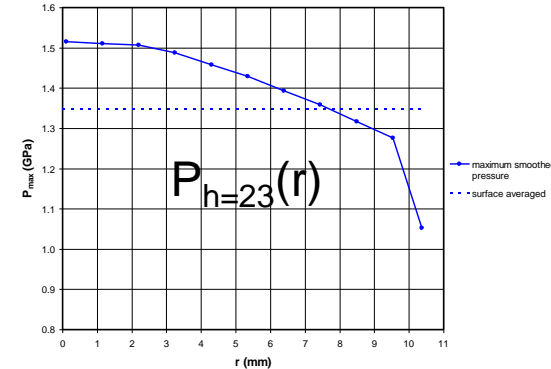
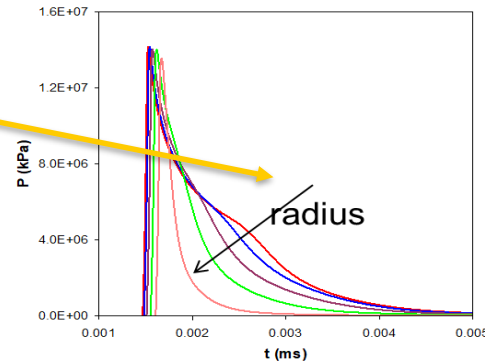
E_c FROM GAP TEST RESULTS (STANAG 4488)

- Two papers looked at relation of E_c and 21 and 50 mm GAP-test results
- Simulation: Pressure at central axis should follow the “calibration curve” as function of gap length h



Surface averaged max. Pressure

$$\overline{P}_{\max} = \frac{1}{\pi R^2} \int 2\pi r P_{\max}(r) dr$$



- *) 1) Ries Verbeek, Richard H. B. Bouma. “Evaluation of the Energy Fluence in the Small Scale Gap Test”, PEP 2011, 36
2) Sebastian Wurster, “Evaluation of the James Initiation Criterion in the 21 mm and 50 mm PMMA Gap Test”, PEP 2017, 42

CALCULATION OF ENERGY FLUENCE AS FUNCTION OF GAP LENGTH h

$$E = \int \overline{P_{max}} \cdot u_{p,x} \cdot dt$$

› Example: in 21 mm gap test a P of 6.25 GPa → $E_c = 4 \text{ MJ/m}^2$

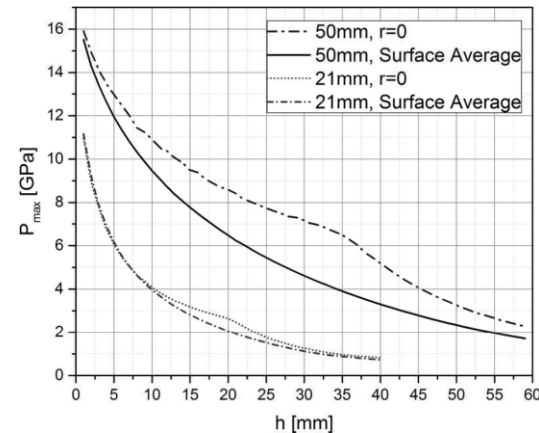


Figure 6. Axial and surface averaged energy fluences as a function of gap length for the 21 mm and 50 mm PMMA gap test.

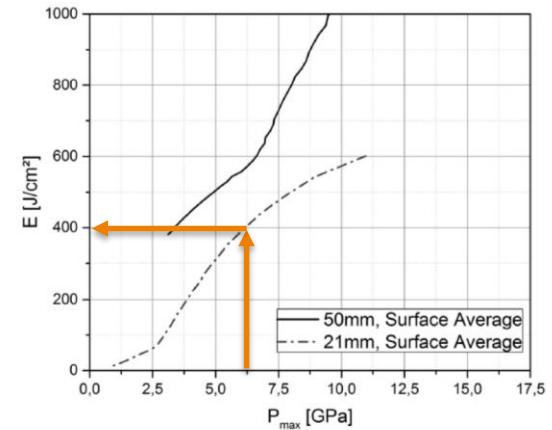
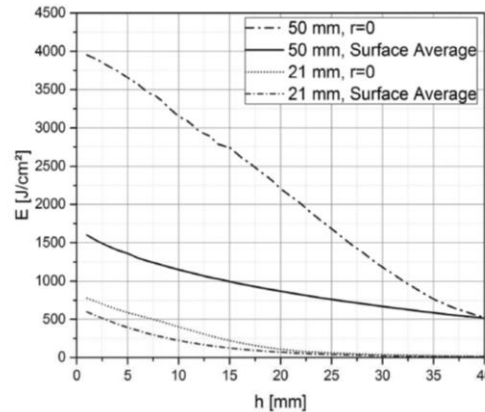
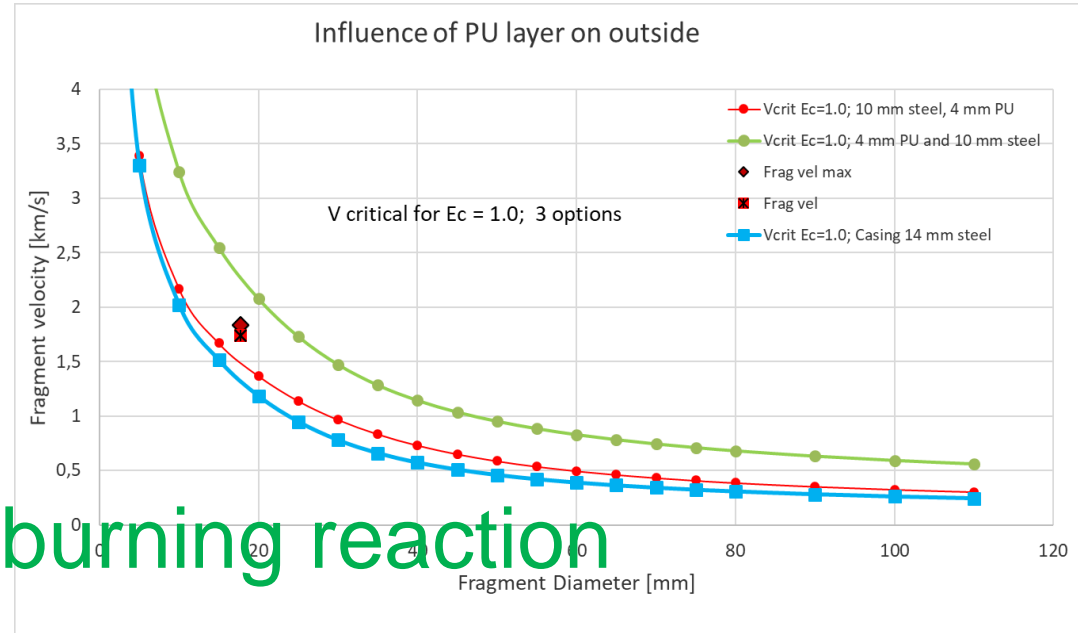


Figure 8. Surface averaged energy fluence as a function of maximum axial pressure in the 21 mm and 50 mm gap test.

NEW MODEL: INFLUENCE OF ADDITIONAL LAYER

- › Advantage of new model: possibility of additional layer! .e.q PU or asphalt
- › Fragment impact on warhead casing 14mm
- › 18 mm steel fragment V~ 1800 m/s
 - › 1) 14 mm steel casing
 - › 2) 10 mm casing with 4 mm PU
 - › 3) 4mm PU in front of 10 mm Steel



Experiments: slow burning reaction

FUTURE: VULNERABILITY TOOLBOX / USER INTERFACE

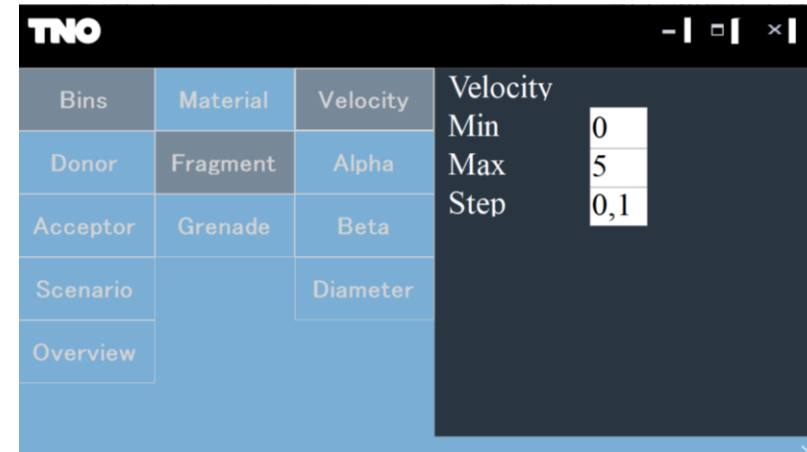
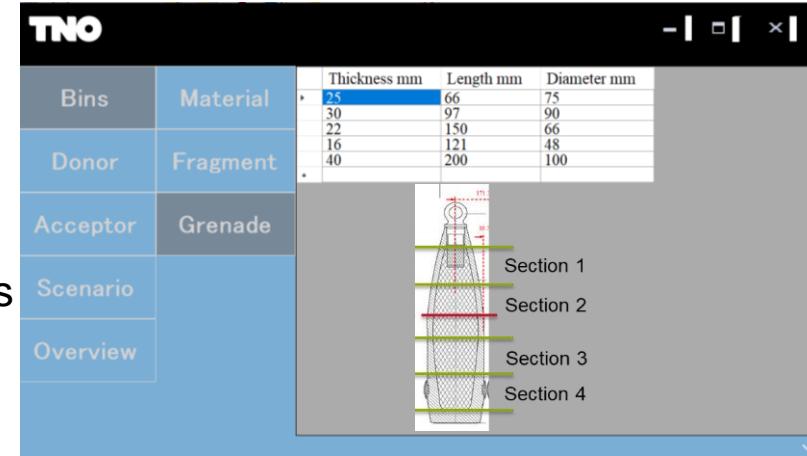


USER INTERFACE

- › Input:
 - › Scenario
 - › Type of munition (incl. sections, materials, sizes and distances, errors)
 - › Model used for SDT calculation (single fragment) . Conf. stack, O-O-O calculation etc.

- › Calculations: drivers/codes for SDT calculation, conf. stack calculation, storage calculation etc.

- › Output: Single fragment output, Storage situation output, Multiple fragment output.....



CONCLUSIONS

- › Improved shock model works very well; follows experimental curves
- › New model has several advantages
 - › Simple and fast calculations using E_c and shock hugoniot of materials
 - › Multi layer target; any material
 - › Also spherical impactor or oblique impact
 - › Can be used in Statistical toolbox for probability calculations
- › Several options to estimate E_c for “unknown” explosives
- › Tool will be implemented in platform vulnerability codes (TARVAC and RESISTS)

Results will contribute to reduction of risks in general and of munitions storage and more balanced ship/vehicle design.



› **THANK YOU FOR YOUR ATTENTION**

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