

9/29/2020

› **TORQUE 2020**

**COMBINED WIND TURBINE DESIGN AND WIND FARM LAYOUT
OPTIMISATION UNDER WIND RESOURCE UNCERTAINTY**

SIDDHARTH KRISHNA SWAMY

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› STUDY OBJECTIVES

- › Combined optimisation of wind turbine design and wind farm layout
- › Optimise turbine rotor diameter
- › Optimise number & position of turbines for a given farm area
- › Optimise orientation of turbines in the farm
- › Optimisation objective: Minimise LCoE, & use uncertainty in wind resource
- › Objective function: TNO Wind Cost Model



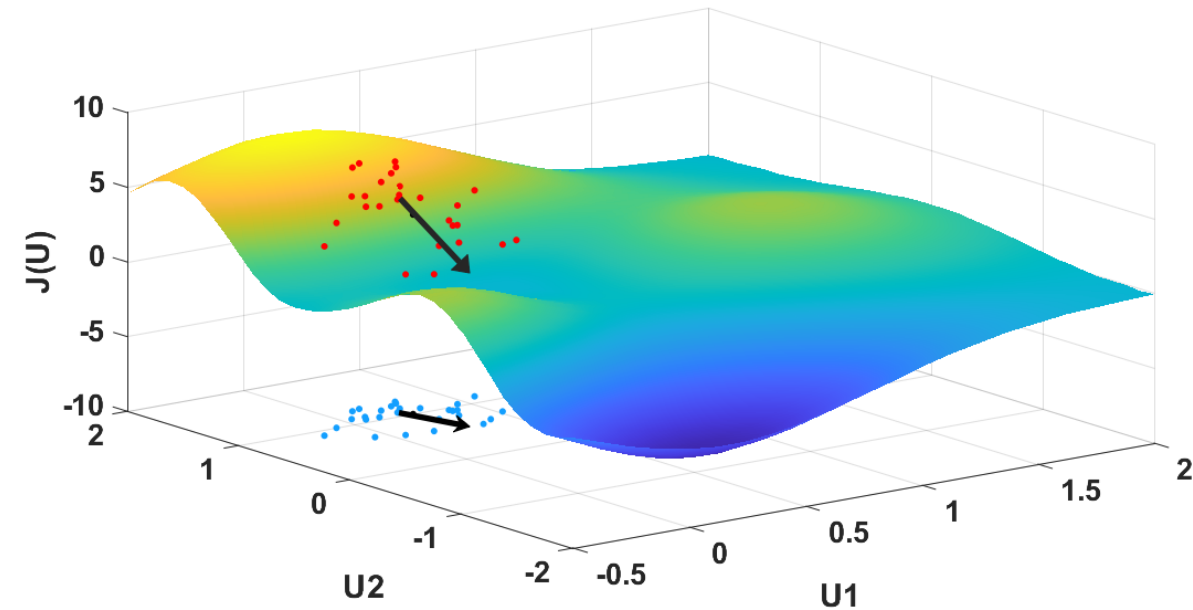
› OPTIMISER

STOCHASTIC SIMPLEX APPROXIMATE GRADIENT (STOSAG)

- › Developed for geological uncertainties for O&G reservoir simulations

Example with two dimensional controls:

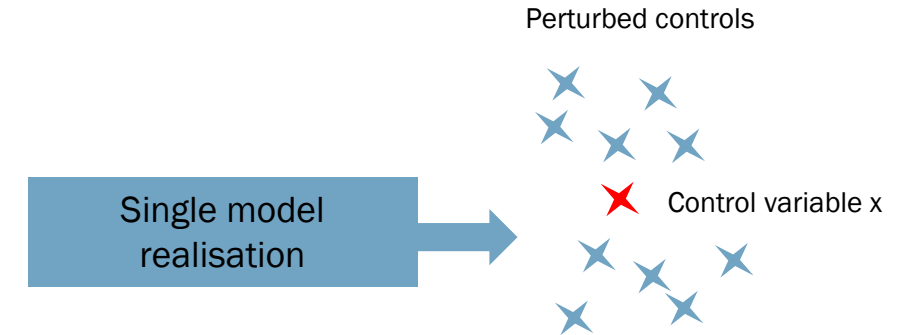
- › Choose an initial set of control variables $(u_1, u_2) = (0.25, 1)$
- › Perturbation of control vectors stochastically (blue dots)
- › Evaluate each perturbed control (red dots)
- › Estimate the gradient using linear regression
- › Update control variables using line search
- › Repeat until convergence.



› STOSAG METHOD

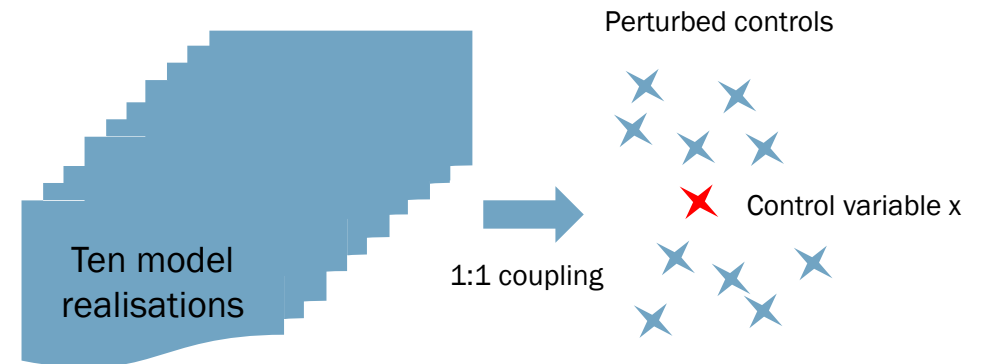
DETERMINISTIC OPTIMISATION

- › No uncertainty, i.e. single model realisation
- › Number of perturbed controls: 10 (for example)
- › Ratio between model realisations and perturbed controls: 1:10

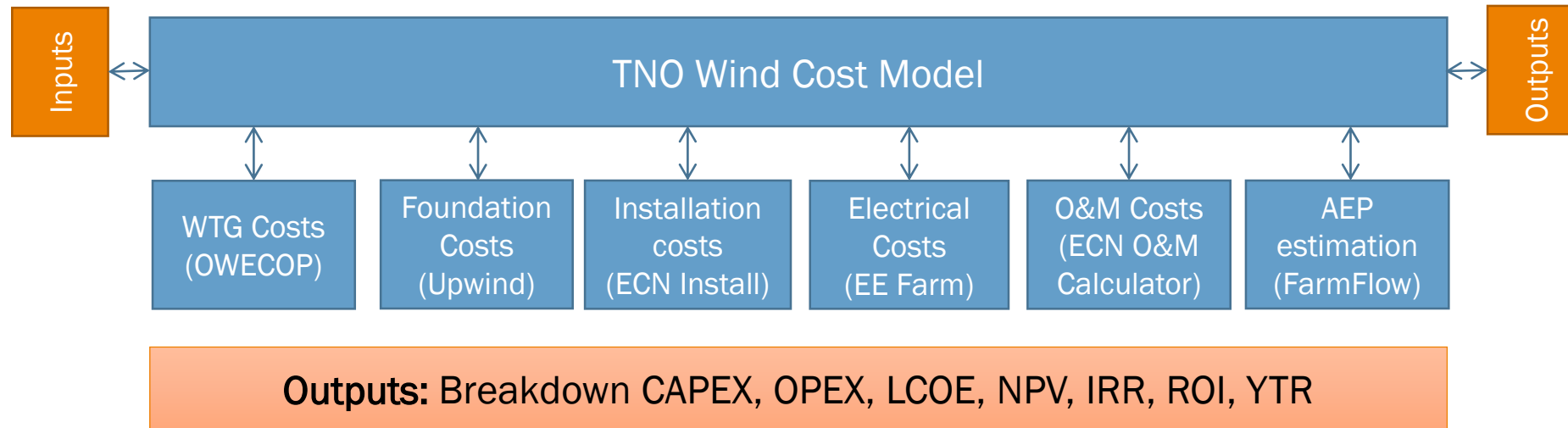


ROBUST OPTIMISATION

- › 10 uncertain model realisations
- › Number of perturbed controls: 10 (as above)
- › One model realisation coupled with one perturbed control
- › Same computational effort as deterministic case



› OBJECTIVE FUNCTION



TNO Wind cost model used for economic evaluation of a “traditional” wind farm:

- › Wind turbine with single rotor
- › Monopile support structure
- › Wind farm in a parallelogram shape (length, width, orientation)
- › Installation and maintenance with SOVs and/or CTVs

$$LCoE = \frac{\left(\frac{CapEx}{a} + OpEx \right)}{AEP}$$

› CONTROL VARIABLES

ROTOR POWER DENSITY (RPD)

- › Unit: W/m²
- › Inversely proportional to square of turbine diameter (d)
- › Turbine rated power fixed (10 MW AVATAR research turbine)

$$RPD = (P_{turbine}) / ((\pi/4)d^2)$$

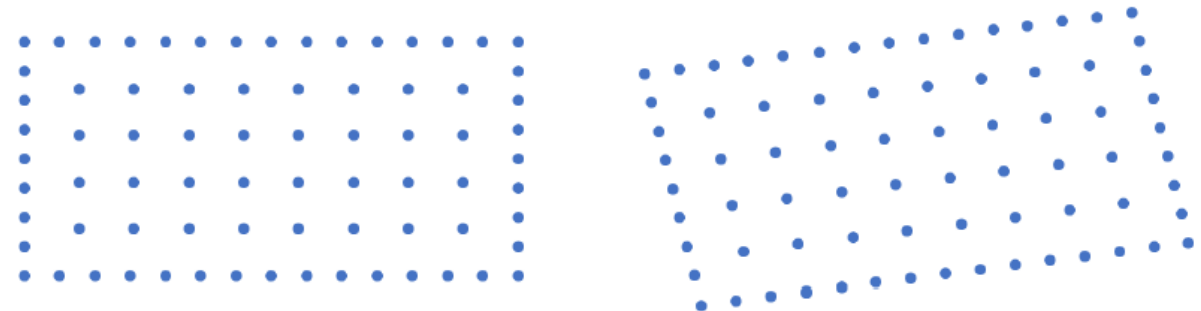
WIND FARM POWER DENSITY (WFPD)

- › Unit: MW/km²
- › Directly proportional to number of turbines in farm
- › Fixed farm area (150 km²)

$$WFPD = (P_{turbine} * n_{turbines}) / A_{farm}$$

FARM ORIENTATION (Θ)

- › Counter clockwise rotation of turbines in the farm



UNCERTAINTY IN WIND RESOURCE

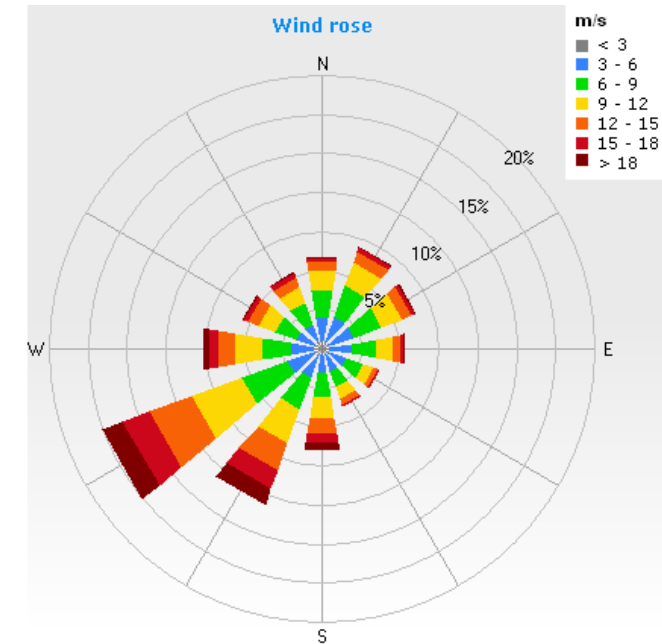
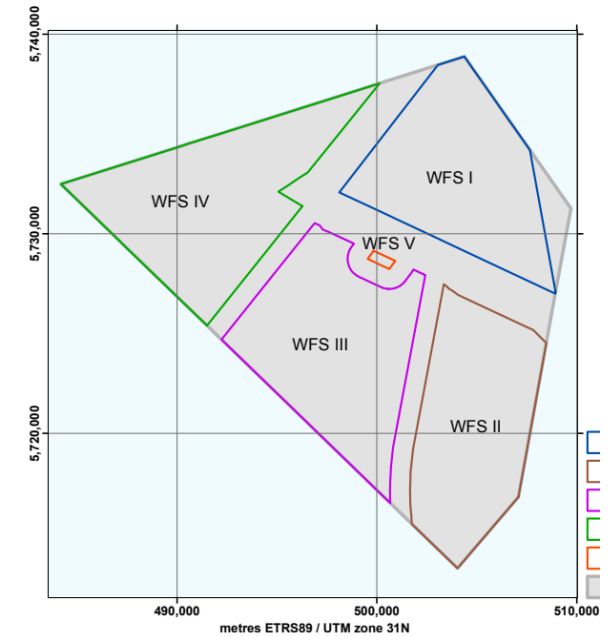
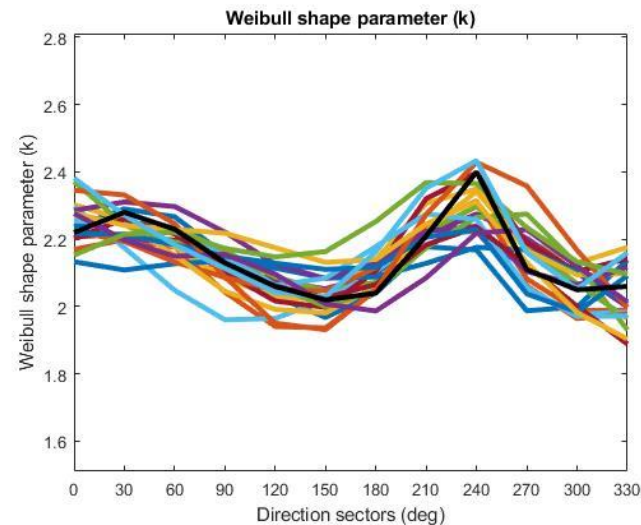
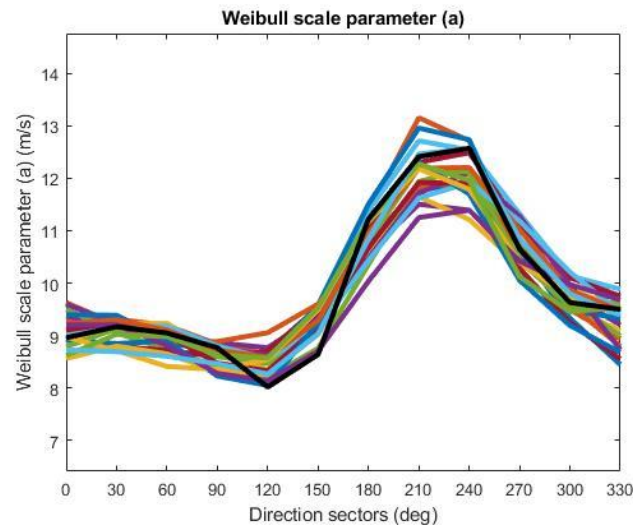
Location:

- › 100m at Borssele Wind farm zone (WFS III)
- › Weibull probability density function:

$$p(U) = (k/a) \left(\frac{U}{a}\right)^{k-1} \exp \left[-\left(\frac{U}{a}\right)^k\right]$$

where scale parameter is (a) and shape parameter is (k)

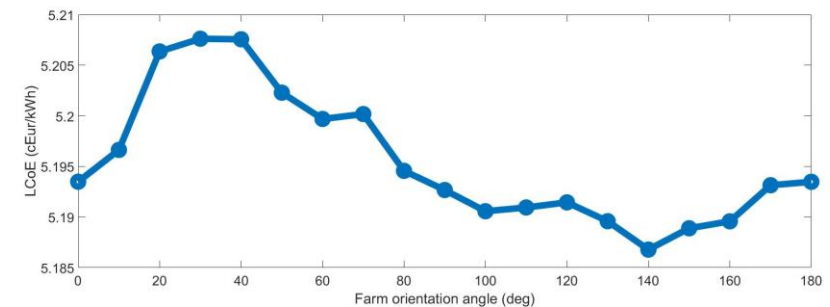
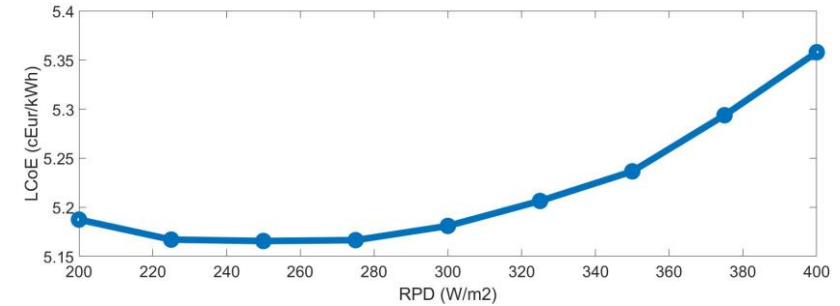
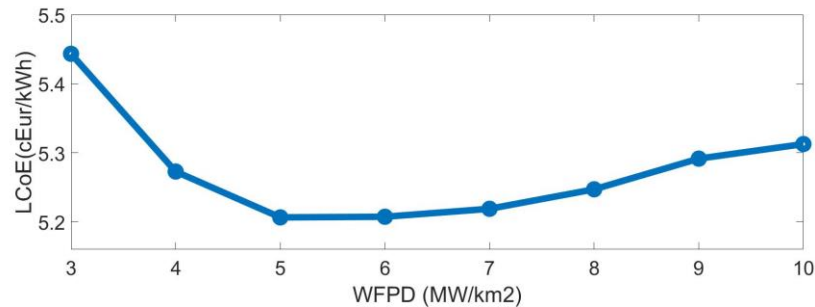
- › 5% uncertainty in Weibull a and k parameters and in each direction sector



› MODELLING

SENSITIVITY ANALYSIS FOR LOWEST LCOE

- › Min. LCoE of ~5.15 c€/kWh
- › @(RPD, WFPD, theta) = (250, 5, 140)



INITIAL CONTROL VARIABLES

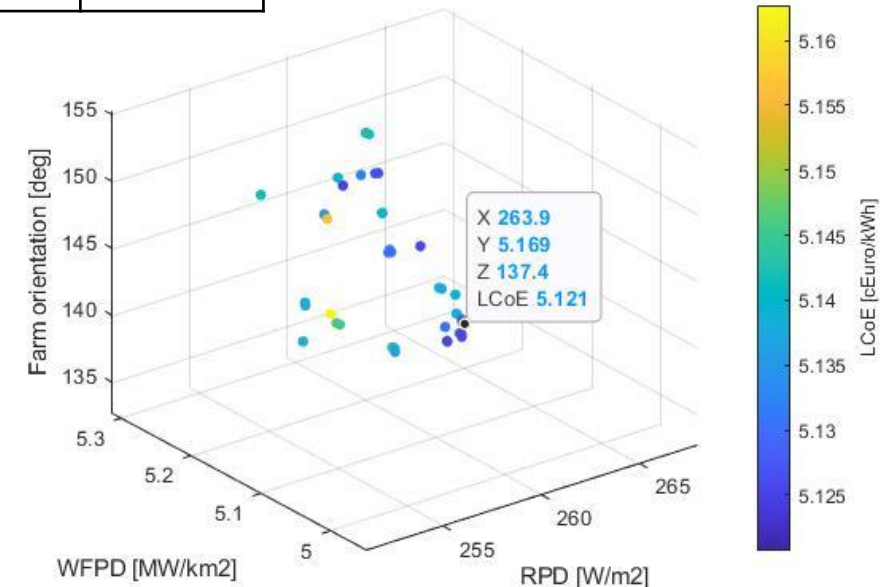
Type	Control variables	RPD (W/m ²)	WFPD (MW/km ²)	Farm angle (°)	Rotor diameter (m)	# turbines	LCoE (c€/kWh)
Deterministic, Robust	2,3	250	5	140	225.7	75	5.144, 5.152

RESULTS

DETERMINISTIC EXPERIMENTS

Type	Control variables	RPD (W/m ²)	WFPD (MW/km ²)	Farm angle (°)	Rotor diameter (m)	# turbines	LCoE (c€/kWh)	% decr. in LCoE
Deterministic	2	265.5	5.178	140	219.0	78	5.125	0.37%
Deterministic	3	263.9	5.171	137.4	219.7	78	5.121	0.45%

- › Farm angle as third control variable decreases LCoE to 0.45%
- › Optimised farm angle (137.4°) gives scope to slightly increase rotor diameter
- › Rotor diameter increased by 0.7m to capture more wind



› RESULTS

ROBUST EXPERIMENTS

Type	Control variables	RPD (W/m ²)	WFPD (MW/km ²)	Farm angle (°)	Rotor diameter (m)	# turbines	Mean LCoE (c€/kWh)	% decr. in mean LCoE
Robust	2	265.1	5.167	140	219.2	78	5.129	0.46%
Robust	3	264.1	5.169	131.9	219.6	78	5.128	0.47%

- › With 2 control variables, 0.46% decrease in mean LCoE
- › Twenty realisations cumulatively orient the wind slightly southwards
- › With 3 control variables, turbine diameter slightly increases

› CONCLUSIONS

- › Optimise turbine design and farm layout
- › Optimised design from deterministic experiments show decrease in LCoE of 0.45%
- › Input uncertainty of 5% in W_a and W_k is reflected with 20 wind resource realisations
- › Robust experiments, with uncertainty, reduce mean LCoE by 0.47%

FURTHER WORK

- › NPV as optimisation objective, with energy integrated market model
- › Estimate uncertainty from historical data by fitting distributions to W_a and W_k
- › Multi-objective optimisation with LCoE and LCA (economic and environmental impact)



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